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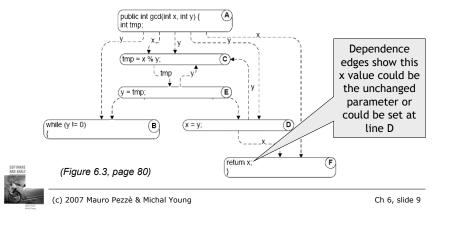
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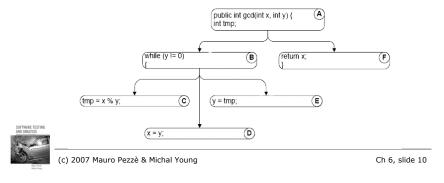
## (Direct) Data Dependence Graph

- A direct data dependence graph is:
  - Nodes: as in the control flow graph (CFG)
  - Edges: def-use (du) pairs, labelled with the variable name



# Control dependence (1)

- Data dependence: Where did these values come from?
- Control dependence: Which statement controls whether this statement executes?
  - Nodes: as in the CFG
  - Edges: unlabelled, from entry/branching points to controlled blocks



#### Dominators

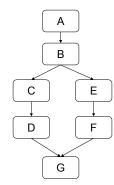
- **Pre-dominators** in a rooted, directed graph can be used to make this intuitive notion of "controlling decision" precise.
- Node M dominates node N if every path from the root to N passes through M.
  - A node will typically have many dominators, but except for the root, there is a unique **immediate dominator** of node N which is closest to N on any path from the root, and which is in turn dominated by all the other dominators of N.
  - Because each node (except the root) has a unique immediate dominator, the immediate dominator relation forms a tree.
- **Post-dominators:** Calculated in the reverse of the control flow graph, using a special "exit" node as the root.



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#### Dominators (example)



- A pre-dominates all nodes; G post-dominates all nodes
- F and G post-dominate E
- G is the immediate postdominator of B
  - C does not post-dominate B
- B is the immediate predominator of G
  - F does not pre-dominate G



#### Control dependence (2)

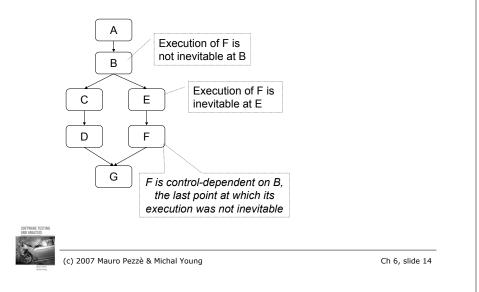
- We can use post-dominators to give a more precise definition of control dependence:
  - Consider again a node N that is reached on some but not all execution paths.
  - There must be some node C with the following property:
    - C has at least two successors in the control flow graph (i.e., it represents a control flow decision);
    - C is not post-dominated by N
    - there is a successor of C in the control flow graph that is postdominated by N.
  - When these conditions are true, we say node N is controldependent on node C.
    - Intuitively: C was the last decision that controlled whether N executed



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#### **Control Dependence**



Data Flow Analysis

#### Computing data flow information



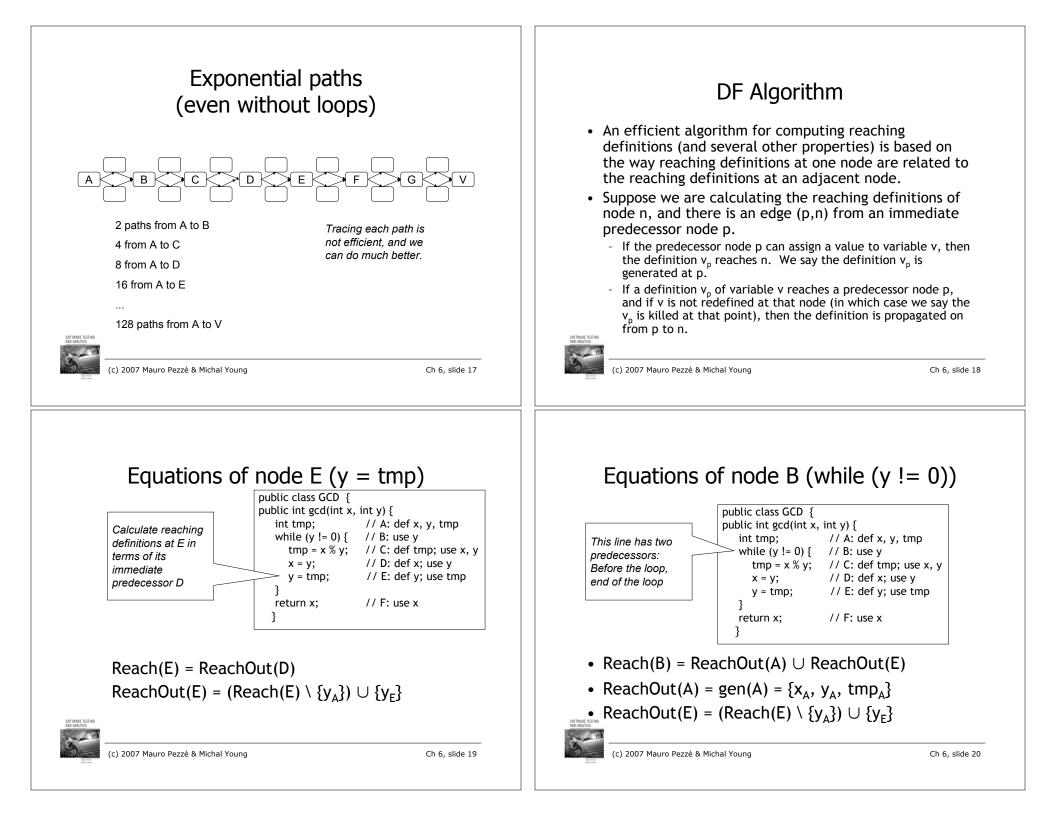
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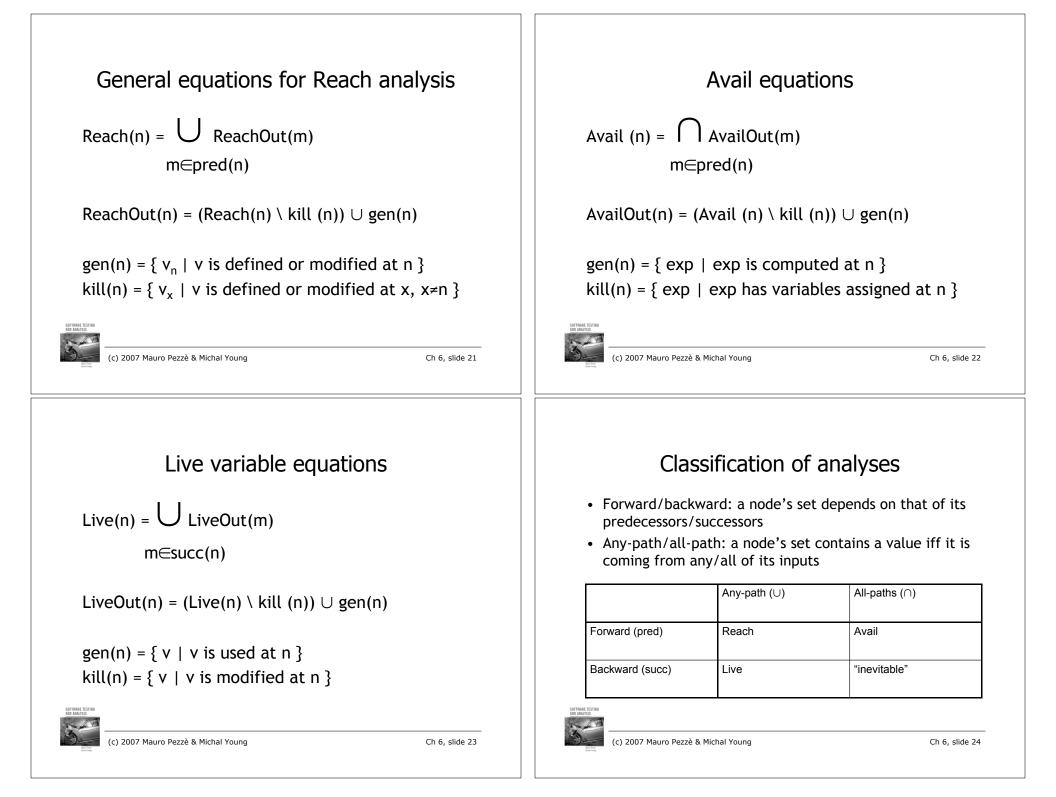
#### Calculating def-use pairs

- Definition-use pairs can be defined in terms of paths in the program control flow graph:
  - There is an association (d,u) between a definition of variable v at d and a use of variable v at u iff
    - there is at least one control flow path from d to u
    - with no intervening definition of v.
  - v<sub>d</sub> reaches u (v<sub>d</sub> is a reaching definition at u).
  - If a control flow path passes through another definition e of the same variable v,  $v_e\, {\rm \bf kills} \, v_d$  at that point.
- Even if we consider only loop-free paths, the number of paths in a graph can be exponentially larger than the number of nodes and edges.
- Practical algorithms therefore do not search every individual path. Instead, they summarize the reaching definitions at a node over all the paths reaching that node.



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#### **Iterative Solution of Dataflow Equations**

- Initialize values (first estimate of answer)
  - For "any path" problems, first guess is "nothing" (empty set) at each node
  - For "all paths" problems, first guess is "everything" (set of all possible values = union of all "gen" sets)
- Repeat until nothing changes
  - Pick some node and recalculate (new estimate)

This will converge on a "fixed point" solution where every new calculation produces the same value as the previous guess.



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## Worklist Algorithm for Data Flow

See figures 6.6, 6.7 on pages 84, 86 of Pezzè & Young One way to iterate to a fixed point solution. General idea:

- · Initially all nodes are on the work list, and have default values
  - Default for "any-path" problem is the empty set, default for "allpath" problem is the set of all possibilities (union of all gen sets)
- While the work list is not empty
  - Pick any node n on work list; remove it from the list
  - Apply the data flow equations for that node to get new values
  - If the new value is changed (from the old value at that node), then
    - Add successors (for forward analysis) or predecessors (for backward analysis) on the work list
- Eventually the work list will be empty (because new computed values = old values for each node) and the algorithm stops.



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# *Cooking your own:* From Execution to Conservative Flow Analysis

- We can use the same data flow algorithms to approximate other dynamic properties
  - Gen set will be "facts that become true here"
  - Kill set will be "facts that are no longer true here"
  - Flow equations will describe propagation
- Example: Taintedness (in web form processing)
  - "Taint": a user-supplied value (e.g., from web form) that has not been validated
  - Gen: we get this value from an untrusted source here



Kill: we validated to make sure the value is proper

## Cooking your own analysis (2)

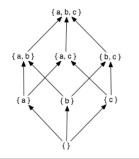
- Flow equations must be monotonic
  - Initialize to the bottom element of a lattice of approximations
  - Each new value that changes must move up the lattice
- Typically: Powerset lattice
  - Bottom is empty set, top is universe
  - Or empty at top for allpaths analysis



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*Monotonic*: y > x implies  $f(y) \ge f(x)$ 

(where f is application of the flow equations on values from successor or predecessor nodes, and ">" is movement up the lattice)



#### Data flow analysis with arrays and pointers

- Arrays and pointers introduce uncertainty: Do different expressions access the same storage?
  - a[i] same as a[k] when i = k
  - a[i] same as b[i] when a = b (aliasing)
- The uncertainty is accomodated depending to the kind of analysis
  - Any-path: gen sets should include all potential aliases and kill set should include only what is definitely modified

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- All-path: vice versa
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#### Scope of Data Flow Analysis

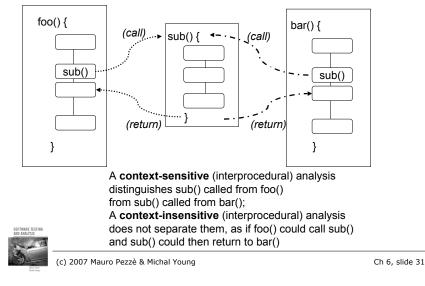
- Intraprocedural
  - Within a single method or procedure
    - as described so far
- Interprocedural
  - Across several methods (and classes) or procedures
- Cost/Precision trade-offs for interprocedural analysis are critical, and difficult
  - context sensitivity
  - flow-sensitivity



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## Flow Sensitivity

- Reach, Avail, etc. were flow-sensitive, in<u>traprocedural analyses</u>
  - They considered ordering and control flow decisions
  - Within a single procedure or method, this is (fairly) cheap  $\mbox{ O}(n^3)$  for n CFG nodes
- Many in<u>ter</u>procedural flow analyses are flowinsensitive
  - O(n<sup>3</sup>) would not be acceptable for all the statements in a program!
    - Though  $\mathsf{O}(n^3)$  on each individual procedure might be ok
  - Often flow-insensitive analysis is good enough ... consider type checking as an example



#### Summary

- Data flow models detect patterns on CFGs:
  - Nodes initiating the pattern
  - Nodes terminating it
  - Nodes that may interrupt it
- Often, but not always, about flow of information (dependence)
- Pros:
  - Can be implemented by efficient iterative algorithms
  - Widely applicable (not just for classic "data flow" properties)
- Limitations:
  - Unable to distinguish feasible from infeasible paths
  - Analyses spanning whole programs (e.g., alias analysis) must trade off precision against computational cost



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